

# Suggested solutions to exam in Applied Electromagnetism 071025

## 1

In the series case

$$C_{tot} = \left( \frac{1}{C} + \frac{1}{C} + \frac{1}{C} \right)^{-1} = \frac{C}{3} \Rightarrow W_{tot,series} = \frac{C_{tot} U^2}{2} = \frac{1}{3} \frac{CU^2}{2}$$

And in the parallel case:

$$C_{tot} = 3C \Rightarrow W_{tot,par} = \frac{C_{tot} U^2}{2} = 3 \frac{CU^2}{2}$$

The energy in the parallel case is nine times the energy in the series case.

If you look at the problem with field energy instead:

E-field has the same volume in both cases but is three times larger in the parallel case. As energy is proportional to  $E^2$ , this means the energy is nine times higher.

## 2

Let  $a = 10\text{mm}$

$$\vec{E} = \frac{2\lambda}{2\pi\epsilon_0 \sqrt{a^2 + x^2}} (\cos\theta, 0, 0) \Rightarrow E_x = \frac{2\lambda x}{2\pi\epsilon_0 (x^2 + a^2)}$$

We look for the max of this:

$$\frac{dE_x}{dx} = \frac{\lambda}{2\pi\epsilon_0} \left( \frac{1}{x^2 + a^2} - \frac{x \cdot 2x}{(x^2 + a^2)^2} \right) = \frac{\lambda}{2\pi\epsilon_0} \frac{a^2 - x^2}{x^2 + a^2} = 0 \Rightarrow x = a$$

The field is zero at  $x=0$  and in infinity so this has to be a max

## 3

The field of a dipole far away (yes  $0.1 \mu\text{m}$  is far away compared to the molecule size around  $0,001 \mu\text{m}$ ) is

$$E_{along} = \frac{P}{2\pi\epsilon_0 r^3} = 108 \text{ V/m increasing the outer field}$$

$$E_{perpendicular} = \frac{P}{4\pi\epsilon_0 r^3} = 54 \text{ V/m decreasing the outer field}$$

## 4

The resistance of a thin slice with thickness  $dz$  is

$$dR = \frac{\rho}{\pi r^2} dz = \frac{a\rho}{\pi b^2 (a + |z|)} dz \Rightarrow R = \frac{2a\rho}{\pi b^2} \int_0^{1,5\text{mm}} \frac{1}{a + z} dz = \frac{2a\rho}{\pi b^2} \left[ \ln\left(\frac{3,5}{2}\right) \right] = 1.07 \Omega$$

$a = 2 \text{ mm}$  and  $b = 0.3 \text{ mm}$ .

Yielding a voltage  $1.28 \text{ V}$

## 5-6

There are a lot of assumptions and approximations you have to do for yourself in this task

First typical speed of the electrons:  $5\text{kV}$  gives a kinetic energy if  $8 \times 10^{-16} \text{ J}$ , giving a velocity of

$4 \times 10^7 \text{ m/s}$ . Now look at an electron travelling towards the center of the screen (does not have to be deflected by the internal magnets) its path gets a radius of curvature of around  $5 \text{ m}$  because of the earths B-field ( $0.00004 \text{ T}$ ). This gives deflected angle on a  $0,5\text{m}$  long path of  $5.7^\circ$ , giving a displacement of around  $2 \text{ cm}$ . You probably have to adjust horizontal position of your TV set if you rotate it  $180^\circ$  if it is not done automatically (it is mostly). But remember this calculation is very coarse!