

## Solutions to Optical Physics 021018

1

The first intermediate image is situated in the field lens and has the size  $h_1 = \alpha f_1$

Where  $\alpha$  is the subtended angle by the object.

The second intermediate image is at  $z = 210\text{mm}$  and has the size

$$h_2 = \frac{60\text{mm}}{30\text{mm}} h_1 = 2\alpha f_1$$

This is situated in the front focal plane of the eye-piece with angle

$$\beta = \frac{h_2}{f_{\text{okular}}} = 2\alpha \frac{f_1}{f_{\text{okular}}} \Rightarrow M_a = \frac{\beta}{\alpha} = 8$$

Ray construction shows that the first lens is aperture stop. Imaging this in lens 2 gives an image in  $z = 160\text{mm}$  ( $M = 0,333$ ), giving object distance  $-10\text{mm}$  to lens 3. Image after lens 3 will be at  $z = 156,7\text{mm}$ , giving an object distance of  $83,3\text{mm}$  to lens 4. Final image = exit pupil  $47\text{mm}$  after last lens.

Size  $40\text{mm} \times 0,333 \times 0,667 \times 0,567 = 5\text{mm}$

3

All wavelengths get a phase shift  $\pi$  because of reflection against denser medium.

The condition for constructive interference will be

$$2nd \cos b = (2m + 1)\lambda$$

$m = 2$  for green light ( $550\text{nm}$ ) gives a phase difference of  $6\pi$  for blue and  $4\pi$  for red. This should be ideal.

$$d = \frac{5\lambda}{2 \cdot 1,8 \cos 23^\circ} = 830\text{nm}$$

4

When everything is OK the Fourier pattern will look like the pattern of a single slit

In a/ it will be the same (translation invariant)

b/ Different assumptions can be made regarding what a knot looks like, but regardless of that light will be scattered in direction parallel to the thread

c/ The pattern will be wider

5

This problem is very similar to that in 3 (with different physical background), with a change in colour, giving  $5\pi$  for yellow as the best phase shift.

6

The coherence function can be written as:

$$\gamma = 0,5 \exp(ik\Delta L) \left\{ 1 + \frac{1}{2} [\exp(i\Delta k\Delta L) + \exp(-i\Delta k\Delta L)] \right\} = \frac{\exp(ik\Delta L)}{2} \left\{ 1 + \cos \frac{2\pi\Delta f\Delta L}{c} \right\}$$

Where the factor in the large parenthesis (including the factor 2) is the visibility

$$V = \frac{1}{2} \left( 1 + \cos \frac{\pi\Delta L}{L_{\text{tas}}} \right)$$